

Photo-induced insulator-metal transition of a spin-electron coupled system

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The photo-induced metal-insulator transition is studied by the numerical simulation of real-time quantum dynamics of a double-exchange model. The spatial and temporal evolutions of the system during the transition have been revealed including (i) the threshold behavior with respect to the intensity and energy of light, (ii) multiplication of particle-hole (p-h) pairs by a p-h pair of high energy, and (iii) the space-time pattern formation such as (a) the stripe controlled by the polarization of light, (b) coexistence of metallic and insulating domains, and (c) dynamical spontaneous symmetry-breaking associated with the spin spiral formation imposed by the conservation of total spin for small energy-dissipation rates.

Changes of electronic states induced by the photo-irradiation have been the subject of intensive studies in chemistry, biology and physics. For example, the photo-induced chemical reactions in molecules are the basis of many biological functions. In solids, the structural changes induced by the absorption of photons and the relaxation after it are a common phenomenon [1]. In particular, in correlated electrons such as the transition metal oxides, the collective nature of the system enhances the sensitivity to the external stimuli including photons, and hence even the weak photo-irradiation can trigger the changes of whole system as the phase transition [2–6]. This is because in strongly correlated electronic systems, the rich phases of spin/charge/orbital orderings with nearly degenerate energies compete with each other [7]. For example, in the case of manganites, colossal magneto-resistance effect occurs because the weak external magnetic field drives a transition from the insulating charge/spin/orbital ordered state to the ferromagnetic metallic state [8], and similar transition can be triggered also by the photo-irradiation [5].

In contrast to these ample examples of photo-induced phase transitions, the theoretical studies are still in the premature stage. Although a classical model for the photo-induced phase transition has been proposed [9], the quantum theory of photo-induced dynamics of correlated electrons are limited to small size systems or to one-dimensional systems [10–12]. Recently, we have proposed a model for the real-time quantum dynamics of correlated electrons, i.e., a double exchange model [13] where the electrons are interacting with the classical spins, to simulate the relaxation after the photo-excitation [14]. In that work, we have developed a theoretical method for the fully quantum-mechanical time-evolution of electronic wavefunction combined with the Landau-Lifshitz-Gilbert (LLG) equation for classical spins, which enables the analysis of the larger-scale/higher-dimensional systems. By that theoretical study, the self-organized space-time structure induced by the quantum transitions during the relaxation has been revealed [14].

In this paper, we present the real-time quantum dynamics of the photo-induced insulator-to-metal (IM) transition for a generalized double exchange model showing the competing antiferromagnetic insulating (AFI) and ferromagnetic metallic (FM) states separated by the first-order phase boundary. Many unexplored issues can be addressed in this model, i.e, the threshold behavior with respect to the intensity/energy of light, the effect of the polarization of light, space-time pattern formation during the transition, the role of the conservation of total spins, and the asymmetry between the two directions of the transition.

We start with the Hamiltonian,

$$\hat{H} = -t \sum_{\langle ij \rangle, s} c_{is}^\dagger c_{js} + h.c. - J_H \sum_{iss'} c_{is}^\dagger c_{is'} \vec{\sigma}_{ss'} \cdot \vec{S}_i \\ + J \sum_{\langle ij \rangle} \vec{S}_i \cdot \vec{S}_j + J_N \sum_{\langle ij \rangle} (\vec{S}_i \cdot \vec{S}_j)^2 \quad (1)$$

where $\langle ij \rangle$ denotes a nearest-neighbor pair, s and s' are indices for electron spin, respectively, and $\vec{\sigma} = (\sigma^x, \sigma^y, \sigma^z)$ are Pauli matrices. The local spins, \vec{S}_i 's, are taken to be classical vectors with magnitude S , and other notations are standard. We consider the half-filled case, i.e., one electron per site. In Eq.(1), we have introduced the biquadratic exchange interaction with coupling

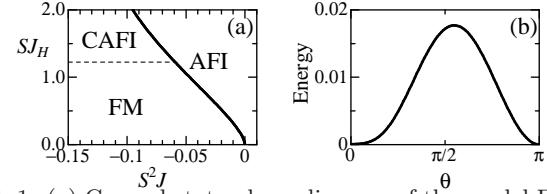


FIG. 1: (a) Ground state phase diagram of the model Eq. (1) in the plane of $S^2 J$ and SJ_H with fixed $S^4 J_N = -0.2$ in units of t . There exist three phases, i.e., ferromagnetic metal (FM), antiferromagnetic insulator (AFI) and canted antiferromagnetic insulator (CAFI). (b) Lowest energy per site measured from ground state as a function of angle between neighboring local-spins in a two sub-lattice consideration on 8×8 system (see text).

constant J_N , which gives an energy barrier between ferromagnetic (F) and antiferromagnetic (AF) states when J_N is negative.

Figure 1(a) shows the ground state phase diagram of the model Eq. (1) on the two-dimensional square lattice, in the plane of $S^2 J$ and SJ_H with fixed $S^4 J_N = -0.2$ in units of t . The solid curve indicates the boundary of first-order phase transition. In the right side, the anti-ferromagnetic spins open a gap and the system is insulating. In the left side, the spins are perfectly or almost ferromagnetic. In the ferromagnetic state, the system is metallic, but the small staggered component opens a small gap for $SJ_H \gtrsim 1.2$ [15]. The phase transition at $SJ_H \approx 1.2$ (broken line) is of the continuous second order.

Let us focus on the boundary of first-order phase transition. Figure 1(b) shows the energy as a function of the angle θ between the sublattice spin directions for 8×8 size system in periodic boundary condition with a parameter set, $t=1$, $SJ_H=1$, $S^2 J=-0.043$, $S^4 J_N=-0.017$, $S=1$. This condition is used hereafter. The AF state and the F state, respectively given by $\theta = \pi$ and 0 , are almost degenerate, and show the local stabilities with the potential barrier between them.

We introduce the Landau-Lifschitz-Gilbert (LLG) equation for the motion of the local spins, $\dot{\vec{S}}_i = \vec{h}_{eff,i} \times \vec{S}_i - \alpha \vec{S}_i \times \dot{\vec{S}}_i$, where $\vec{h}_{eff,i} = \langle \Phi(T) | -\partial \hat{H} / \partial \vec{S}_i | \Phi(T) \rangle$ with $|\Phi(T)\rangle$ being the electronic wavefunction of a Slater determinant at time T obtained by solving the Schrödinger equation as discussed in Ref. [14]. The Gilbert damping constant $S\alpha$ describes all the other relaxation processes of the spins than the coupling to the conduction electrons.

Figure 2 shows time-evolution of the photo-excited electronic state and its relaxation dynamics for $S\alpha = 1$. The unit of time T is \hbar/t and hence is typically $\sim 10^{-15}$ sec assuming $t = 0.4$ eV. We start with the AFI state, i.e., the electronic state has an insulating energy-gap $2SJ_H$ and lower energy band is occupied by electrons and the upper energy band is empty at $T = 0$. In order to mimic the thermal fluctuation, we introduce a random tilting of each spin from the perfect AF configuration up to 0.1 rad which corresponds to the state with an excitation energy of $\sim 0.0003t$ from the ground state. The photo-excitation is achieved by introducing the time-dependent vector potential into the hopping matrix element: for the nearest-neighbor pair $\langle ij \rangle$ in y -direction, we use $t \rightarrow te^{iA(T)}$ where the phase $A(T)$ of the hopping matrix element is given by the vector potential. In the early stage, $T = 0 \sim 80$, we have applied $A(T) = 0.1 \sin(\omega T)$ in this simulation. The frequency ω is tuned for the energy difference between the second highest and the second lowest energy levels of the AF state on the finite size system. The particles are excited from lower to upper energy band (see Fig. 2(a)) and the particle-hole (p-h) pairs are created on the second highest and the second lowest energy levels (see Fig. 2(b)). In the excited state, the spatial distribution of excitation energy is uniform as

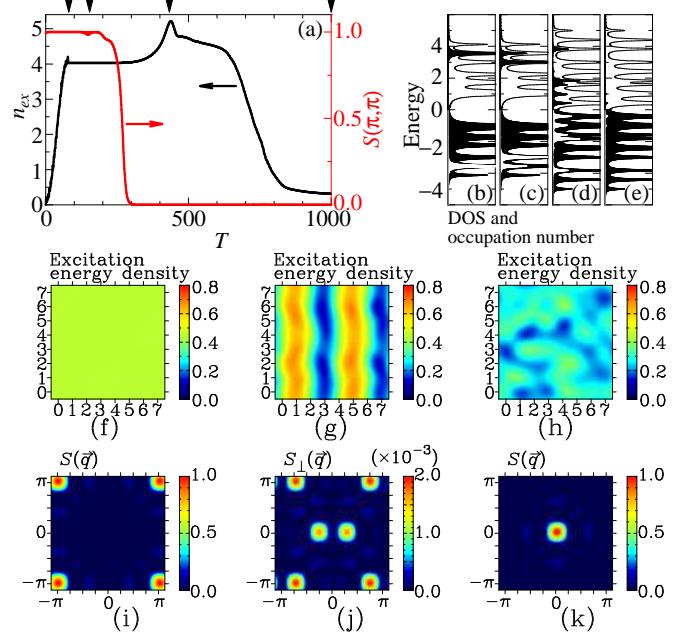


FIG. 2: (Color online) Time evolution of the photo-excited electronic state and its relaxation dynamics for $S\alpha = 1$. (a) Black line with scale on left axis is the time dependence of total occupation number above Fermi level, n_{ex} . Red (gray in print) line with scale on right axis shows the time dependence of the equal-time spin-structure-factor, defined by $S(\vec{q}) = \frac{1}{N} \sum_{ij} \vec{S}_i \cdot \vec{S}_j e^{i\vec{q} \cdot (\vec{i} - \vec{j})}$, for $\vec{q} = (\pi, \pi)$, where \vec{i} and \vec{j} are the vector representation of the lattice points i and j , respectively, \vec{q} is that of the reciprocal lattice-point, and N denotes the system size. The arrows on top axis are the marks for $T = 80, 152, 430$ and 1000 , respectively. (b) Electron occupancy at $T = 80$ represented by the black area with the density of states (DOS) (thin line). The Fermi energy is taken to be zero. In the same way, the electron occupancy at $T = 152, 430$ and 1000 are shown in (c), (d) and (e), respectively. Figures (f), (g) and (h) are the distribution of excitation-energy-density in real space measured from the ground state at $T = 80, 152$, and 430 , respectively. Numbers on horizontal (vertical) axis is for the coordinates of lattice points in x (y) direction. (i) $S(\vec{q})$ at $T = 80$. (j) Transverse component of the equal-time spin-structure-factor $S_{\perp}(\vec{q})$ at $T = 152$. (k) The same with (i) but $T = 430$. A spline interpolation is used for figures (f)-(k).

seen in Fig. 2(f). At $T = 80$, total amount of the excited electron is about 4, and after that, $A(T) = 0$.

Up to $T \sim 200$, the local-spin structure is almost AF one, so that the density of states (DOS) hardly changes as shown by thin lines in Fig. 2(b) and (c). However, the electronic state has been changed dramatically, i.e., the electron occupation shows a time evolution and the spatial distribution of excitation energy forms a stripe pattern as seen in Figs. 2(c) and (g). Correspondingly, the transverse component of the local-spins shows a dynamical pattern as in Fig. 2(j). During the photo-excitation by the light polarized in y direction, the electrons are accelerated along the direction. The polarized motion of electrons derives a deformation of the local-spin structure to be favorable for the electron motion. The charac-

teristics of the relaxation dynamics appear in the *stripe* pattern as seen in Fig. 2(g) reflecting the wave function and the spatial distribution of the excited p-h pairs.

In the period $T = 200 \sim 300$, the system shows a drastic change, that is, AFI to FM transition. For $T < 200$, the spin-structure-factor $S(\pi, \pi)$ is almost 1, and we clearly see the insulating energy-gap $2SJ_H$ between upper and lower energy bands, i.e., the system is the (excited) AFI. For $T > 300$, on the other hand, $S(\pi, \pi)$ is almost 0, and the gap closes. In fact, the energy level structure is very close to that of the tight-binding Hamiltonian for free-electrons with a Zeeman splitting. (The sparse energy level distribution around zero in energy axis is due to the finite-size effect.) As seen in Fig. 2(k), the local-spin becomes the F state corresponding to the metallic electronic-states. The electrons, however, remain still highly excited. As seen in Figs. 2(a) and (d), the total number of excited electrons above Fermi level increases and shows a peak at $T \sim 430$. After that, it decreases but is as large as the number of initially excited electrons, up to $T \sim 660$. On the other hand, it has been confirmed that the total energy of the system, i.e., the electrons and the local spins, decreases monotonically due to the Gilbert damping.

The enhancement of the total number of excited electrons above Fermi level is due to the *Auger process*. This is a characteristics of the interacting electron systems, and is in sharp contrast to the relaxation dynamics of conventional semiconductors which physics is well described by the single carrier problem. This multiplication of p-h pairs during the relaxation dynamics offers an interesting possibility to enhance the photo-current generation and solar cell reaction.

This AFI-to-FM transition, however, does not occur when the excitation is not strong enough. For the results shown in Fig. 2, the photo-excitation has been done in the early stage, $0 \leq T \leq T_f = 80$, with $\omega \cong 7SJ_H$. By decreasing the period T_f , we can reduce the number of the p-h pairs by the photo-excitation $n_{ex}(T_f)$. We find that the IM transition hardly occurs for $n_{ex}(T_f) \lesssim 2$, in the present numerical condition.

We have also examined the frequency ω dependence for the IM transition. In the case that $\omega = 2SJ_H$, the threshold of the IM transition is lying on $4 < n_{ex}(T_f) < 5$ in the numerical simulations. Although the IM transition occurs even in this case, we do not find the Auger process. Comparison with the above case of $\omega \cong 7SJ_H$, it is concluded that the higher energy photon is more effective to induce the IM transition through the Auger process.

When $n_{ex}(T_f)$ is close to the threshold, we find the coexistence of the insulating and metallic domains. The results for $\omega = 2SJ_H$ and $n_{ex}(T_f) \simeq 4.13$ are summarized in Fig. 3. The local-spin state changes gradually in a long time period, $150 \lesssim T \lesssim 1100$ (see the time dependence of $S(\pi, \pi)$ in Fig. 3(a)). A long time later, the AF (blue) and F (yellow) domains are spatially separated as seen in Fig. 3 (d), and the corresponding excitation energy density is shown in Figs. 3 (e). The energy levels and

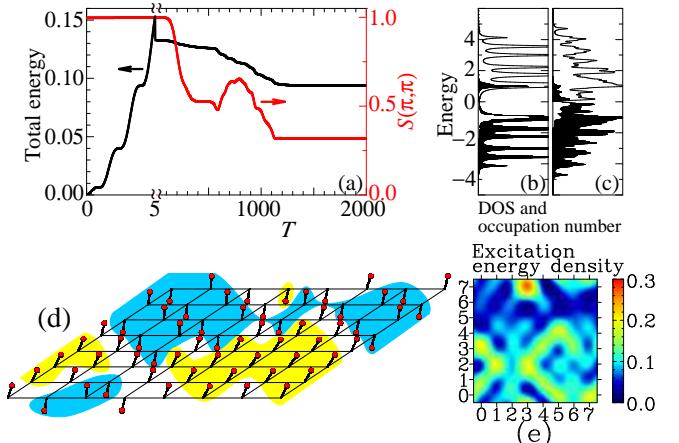


FIG. 3: (Color online) (a) Black line with scale on left axis is the time dependence of total energy per site measured from ground state. Red (gray in print) line with scale on right axis shows $S(\pi, \pi)$ as a function of T . For the photo-excitation, $A(T) = 0.15 \sin(2SJ_H T)$ is used. Different time scales are used for $T < 5$ and $5 < T$, respectively, to zoom up the initial stage for the photo-excitation. During the photo-excitation, total energy increases, and later on ($5 < T$) it decreases due to the Gilbert damping. (b) The same with Fig. 2(b) but $T = 6$ in this simulation. (c) The same with (b) but $T = 2000$. (d) Local spin structure at $T = 2000$. The stick with dot indicates the local spins. There exist AF and F domains. The F and AF domains are expressed by yellow (gray) and blue (dark gray) regions, respectively. In the figure, the spin belongs to F (AF) domain when all the neighboring spins are in F (AF) alignment, and the other spins are put into the white area. (e) The same with Fig. 2(f) but $T = 2000$ in this simulation.

occupation numbers before and after the transition are shown in Figs. 3(b) and (c), respectively. The residual p-h pairs in Fig. 3 (c) are confined in the F metallic domain, so that the electronic state form a slightly higher energy density region on the F domain and the stable AFI domain (see Figs. 3(d) and (e)). This meta-stable state continues for a long time within our simulation (at least up to $T \sim 6000$).

We have also studied the more realistic case of $S\alpha=0.01$ (Fig. 4). Other parameters are the same with the case shown in Fig. 2. Due to the reduced relaxation rate, it takes much longer time for whole relaxation dynamics compared with that in Fig. 2. Despite the reduced relaxation rate, the real-time dynamics of the electronic and local-spin states is not silent and is rather active. During the relaxation dynamics, the direction of the staggered magnetization changes drastically. And the spatial inhomogeneity of the electronic state has also been developed (see Fig. 4(f)). The slow energy relaxation is advantageous for the Auger process resulting in the large amount of p-h pair creation at $T \sim 8000$ when the gap closing occurs (see Fig. 4(a)). At this transition, all the local-spins play very active dynamics with developing spatial inhomogeneity of the electronic state (see Fig. 4(g)). The change of spin configuration from AF state is clearly seen in the equal-time spin-structure-factor shown in Figs. 4(a) and (j): The intensity at (π, π)

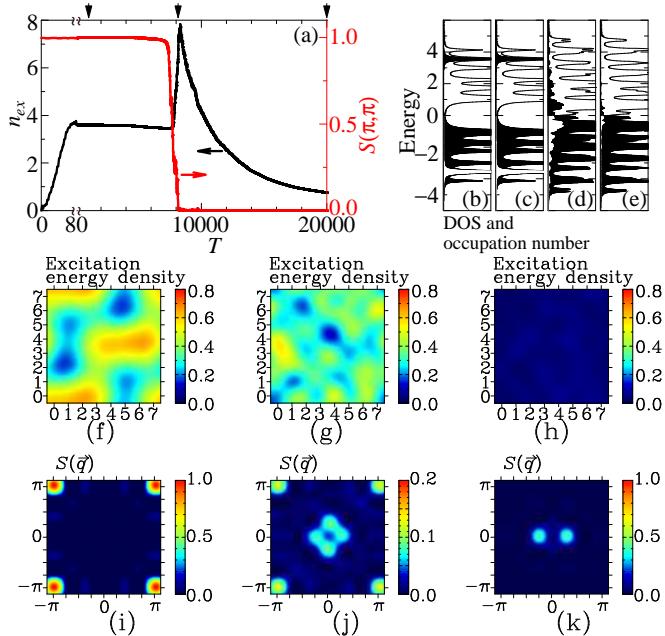


FIG. 4: (Color online) The same with Fig. 2 but $S\alpha = 0.01$ is used. In (a), different time scales are used for $T < 80$ and $80 < T$, respectively, to zoom up the initial stage. The arrows on top axis are the marks for $T = 1000, 8110$ and 20000 , respectively. Figure (b) is the same with Fig. 2(b) but $S\alpha = 0.01$. The figures (c), (f) and (i) show the results at $T=1000$. The figures (d), (g) and (j) show the results at $T=8110$. Here, $S(\vec{q})$ is presented on (j), instead of $S_{\perp}(\vec{q})$. The figures (e), (h) and (k) show the results at $T=20000$.

becomes small and that at around the center region is grown. Near the center, there exist four spots, and two of them disappear later on in the time evolution. Finally, a *spiral* spin-structure is obtained in this case (see Fig. 4(k)). Due to the Gilbert damping $S\alpha$, the total spin-angular-momentum can change in the relaxation dynamics. For large $S\alpha$ the spin state can be easily changed from AF to F as in Fig. 2(g) but not for small $S\alpha$ because the conservation law becomes effective. Therefore, the ferromagnetic state is avoided and the *spiral* spin configuration appears characterized by the equal-time spin-structure-factor shown in Fig. 4(k). In the present case, the propagation vector of the *spiral* spin-state is in x di-

rection. This is the dynamical symmetry breaking, and the direction (x in this particular case) is chosen by the accidental reason while the memory of the polarization of photo-excitation (y direction) has been already lost.

So far, we have discussed the AFI-to-FM transition. As shown in Fig. 1(b), FM and AFI states are almost degenerate, so that FM-to-AFI transition of this system is worth to be examined. In the F state, however, the excitation with $\vec{q} = 0$ is prohibited. Therefore, we have prepared the initial excited-state within F state by putting the initial electron occupation by "hand". Although we have examined a number of numerical simulations, metal-to-insulator transition has not been obtained. The numerical results suggest that metal-to-insulator transition is much more difficult than insulator-to-metal transition in the present model.

In summary, we have studied the insulator-to-metal transition by the photo-irradiation in a model of competing AF and F states. (i) The threshold behavior with respect to the intensity and energy of lights, (ii) Auger process, i.e., multiplication of particle-hole (p-h) pairs by a p-h pair of high energy, (iii) the space-time pattern formation including the stripe controlled by the polarization of light, and (iv) the intriguing spin spiral state by the conservation of total spin for weak Gilbert damping have been revealed. The photo-carrier generation under the external electric field and its implications to the solar cell reaction are the issues left for future studies.

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